TECHNICAL NOTE

No. 950

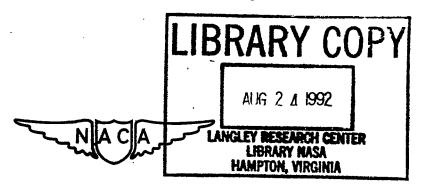
HUMERICAL PROCEDURES FOR THE CALCULATION

OF THE STRESSES IN MONOCCQUES

II - DIFFUSION OF TENSILE STRINGER LOADS

IN REINFORCED FLAT PANELS WITH CUT-OUTS

By N. J. Hoff and Joseph Kempner Polytechnic Institute of Brocklyn



Washington frovember 1944

NATIONAL ADVISORY COMMITTEE FOR AERONAUTICS

TECHNICAL NOTE NO. 950

NUMERICAL PROCEDURES FOR THE CALCULATION

OF THE STRESSES IN MONOCOQUES

II - DIFFUSION OF TENSICE STRINGER LOADS IN REINFORCED

FLAT PANELS WITH CUT-OUTS

By N. J. Hoff and Joseph Kempner

SUMMARY

Experiments were carried out at the Polytechnic Institute of Brooklyn with a flat reinforced sheet model the longitudinals of which were loaded axially. In the first group of tests one panel of sheet, and in the second group two panels of sheet and the intervening portion of a stringer, were cut out. The stress distribution in stringers and sheet was measured with electric strain gages. The stresses were then calculated with the aid of a procedure of successive approximations similar to the one presented in NACA TN No. 934 (reference 1). The agreement between calculations and experiment was found to be reasonably good.

INTRODUCTION

The methods of and the formulas used in the analysis of monoccque aircraft structures have been developed almost invariably for cylinders of circular, or possibly elliptic, cross section and of uniform mechanical properties. Yet in actual aircraft such structural elements are seldom, if over, found. Unfortunately, the direct methods of analysis are little suited to cope with the problems involving complex cross-sectional shapes, irregular distribution of reinforcing elements, concentrated loads, and cut-outs. It is believed that the indirect methods recently advanced by Hardy Cross, and particularly by R. V. Southwell, (references 2 and 3) promise a solution of such problems.

In this indirect approach the stress distribution in a

structure under specified loads is determined through stepby-step approximations. In each step the state of distortion of the structure is arbitrarily modified and the
stresses corresponding to the distortions are calculated.
The procedure must be continued until the stresses and the
external loads over the entire structure are in equilibrium.
When the steps are undertaken at random, the procedure is
likely to lead to a solution only, if ever, after a very
great number of steps. If the calculations are to be well
convergent — that is, if a reasonably rapid approach to the
final state of distortion is to be attained — the steps
must be undertaken according to suitable predetermined patterns. This is the reason Southwell called the procedure
the Method of Systematic Relaxations.

It is the object of the present investigations to develop patterns which make a solution possible, with engineering accuracy, through a limited number of steps. This end is approached by means of theoretical considerations, strain measurements, and comparative calculations. The immediate goal is to work out a procedure which permits the solution of the complex problems previously mentioned, even though approximate results are all that may be attained for the time being.

The procedure can be refined so that it will give more accurate results. It is planned to carry out this development after the more immediate problems are solved.

In this second report experiments are described which were performed in the Aircraft Structures Laboratory of the Polytechnic Institute of Brooklyn with two flat sheet—stringer combinations each having a cut—out. The stress distribution under concentrated loads was investigated with the aid of Baldwin—Southwark Metalectric strain gages. Displacement patterns were developed for the step—by—step procedure the use of which permits a rapid convergence of the computations. The results of the calculations were in reasonably good agreement with the tests.

This investigation, conducted at the Polytechnic Institute of Brooklyn, was sponsored by and conducted with the financial assistance of the National Advisory Committee for Aeronautics. For his aid in the tests and the calculations credit is due Ivan P. Villalba.

SYMBOLS

3

- h distance between adjacent transverse reinforcements
- t thickness of sheet
- u horizontal displacement

u hlock horizontal block displacement

un horizontal displacement of point N

un tot total horizontal displacement of point N

v vertical displacement

v_{block} vertical block displacement

 v_N vertical displacement of point N

vn total vertical d'isplacement of point N

x, y corrdinates

influence coefficient signifying a force in the x-direction at the point M due to a unit X displacement of point N

xymn influence coefficient signifying a force in the x-direction at point M due to a unit y displacement of point N

YYMN influence coefficient signifying a force in the ydirection at point M due to a unit y displacement of point N

yxmn influence coefficient signifying a force in the ydirection at point M due to a unit x displacement of point N

Atot total effective cross-sectional area of a stringer

A-Q symbols used to designate points of intersection of longitudinal and transverse reinforcements

B, M, T symbols used to designate bottom, middle, and top horizontal sections, respectively, of model

- B' location of point B after displacement
- E modulus of elasticity
- G modulus of elasticity in shear
- K numerical constant
- L length
 - LMN distance between points M and N
 - σx direct stress in horizontal reinforcing strip
 - σ_v direct stress in vertical reinforcing strip
 - 1 36 symbols used to designate strain gages
 - I IV symbols used to designate stringers

EXPERIMENTAL INVESTIGATIONS

The test model shown in figure 1 consisted of a flat sheet of 24 S-T aluminum alloy reinforced with longitudinally and transversely arranged steel strips. The model was the one used for the experiments described in reference 1, but for the first group of the present tests one panel of sheet, for the second group of tests two panels of sheet and the intervening portion of a stringer, were removed. The resulting structures will be referred to as "model with single cut-out," and "model with double cut-out," respectively.

The test apparatus was the same as that used for the experiments described in reference 1. Equal tensile forces applied at the four botton stringer extensions were balanced by equal tensile forces at the two top stringer extensions. The double cut-out condition of the model is shown in the photographs of figures 2 and 3. Two angle irons were used to prevent the lower edge of the cut-out from buckling. These acted like the lugs described in reference 1 which supported the upper edge of the model. A lubricated sliding contact between a fitting at the end of the angle irons and the lower edge of the cut-out prevented restraint in the plane of the sheet.

Loads and strains were measured with Baldwin-Southwark Metalectric strain gages. No details of the measuring technique need be given here since the procedure followed was the same as that described in reference 1. The square of aluminum and steel to which the dummy gages were cemented is clearly visible in figure 2. Tests were performed on the model with single cut-out at load increments of 240 and 496 pounds, and on the model with double cut-out at load increments of 248 and 492 pounds. A tare load of 240 pounds was used for all tests. Since the stresses obtained for the higher load conditions were practically double those of the lower, the lower load condition only was used for comparison of experimental and calculated stresses.

The experimental data were analyzed in the same manner as in reference 1. For all stress calculations the modulus of elasticity was taken as 30 \times 10⁶ psi and 10.3 \times 10⁶ psi for steel and aluminum, respectively.

The total effective width of sheet for both model conditions was taken as that obtained for the flat sheet in. reference 1: namely, 6.72 inches. As was done previously the overlapped portions of the sheet at the central stringers were assumed fully effective in carrying normal stresses. Consequently, the average total effective area of a vertical or horizontal edge stringer was found to be 0.1301 square inch, that of a central vertical stringer 0.1418 square inch, and that of a central horizontal strip 0.1381 square inch. For the stringers adjacent to the cut-out these values were necessarily modified to 0.1256 and 0.1337 square inch for segments HM and GL, respectively (see fig. 7) and to 0.1301 square inch for strips GH and LM, because of the absence of panel GHML. Similar changes also were made when the model with the double cut-out was considered. The values for FK, FG, and KL (see fig. 8) became 0.1337, 0.1301, and 0.1301 square inch, respectively. It should be noted that the areas of effective width of the aluminum sheet had been converted into equivalent areas of steel.

The values given in the preceding paragraph will be used later for the calculation of the influence coefficients needed for the relaxation procedure.

DERIVATION OF THE FORMULAS USED IN THE SUCCESSIVE APPROXIMATIONS PROCEDURE

As in reference 1, the unit of the elastic structure considered in this paper consists of a panel of sheet metal and the four segments of bars fastened to its edges (fig. 4). It is assumed that the bars are attached to one another by ideal pins and that they have infinite rigidity in bending. In reference 1 only the forces acting in the vertical (y) direction were taken into account. Consideration of the horizontal forces was unnecessary because of the symmetry of the structure and loading about a vertical axis. the present investigations, the loads are still applied symmetrically, but the symmetry of the structure is destroyed by the cut-outs. Consequently, it is necessary to calculate the equilibrium of the horizontal forces acting in the structure, and thus two more types of influence coefficients must be developed in addition to the Ty influence coefficients derived in reference 1.

It follows from the derivations presented in reference 1 that the \widehat{yy} influence coefficients pertaining to point B of figure 4a — that is, the vertical forces transmitted to the constraints at points A, B, C, and D when point B is moved through a unit distance in the positive y direction — can be given by the following equations:

$$\widehat{yy}_{AB} = \widehat{yy}_{DB} = Gth/4b$$

$$\widehat{yy}_{CB} = EA_{tot}/h - Gth/4b \qquad (1)$$

$$\widehat{yy}_{BB} = -(EA_{tot}/h + Gth/4b)$$

It is obvious that a horizontal force arising from a unit horizontal displacement is analogous to a vertical force arising from a unit vertical displacement. Consequently, if point B in figure 4 is displaced through a unit distance in the positive x-direction, the following influence coefficients apply:

$$\widehat{xx}_{AB} = (EA_{tot}/b - Gtb/4h)$$

$$\widehat{xx}_{CB} = \widehat{xx}_{DB} = Gtb/4h$$

$$\widehat{xx}_{BB} = -(EA_{tot}/b + Gtb/4h)$$
(2)

It should be noted that the quantities Gtb/4h and Gth/4b are unit forces caused by the resistance of the sheet to shearing deformations. By the law of the complementary shearing stress, however, horizontal displacements also must give rise to vertical shearing forces, and vertical displacements to horizontal shearing forces. Consequently, there are couplings between quantities pertaining to the vertical and the horizontal directions which can be expressed by xy and yx influence coeficients. Those corresponding to a displacement of point B as shown in figure 4b are given by the following equations:

$$\widehat{yx}_{CB} = \widehat{yx}_{BB} = Gt/4$$

$$\widehat{yx}_{AB} = \widehat{yx}_{DB} = -Gt/4$$
(3)

Similarly, through the consideration of the effects of a unit vertical displacement of point B the following formulas can be derived:

$$\widehat{\mathbf{x}}\widehat{\mathbf{y}}_{CB} = \widehat{\mathbf{x}}\widehat{\mathbf{y}}_{DB} = -Gt/4$$

$$\widehat{\mathbf{x}}\widehat{\mathbf{y}}_{AB} = \widehat{\mathbf{x}}\widehat{\mathbf{y}}_{BB} = Gt/4.$$
(4)

When the structure consists of several panels as in figure 5, the effect of all of them must be taken into account simultaneously. Therefore, the following influence coefficients can be calculated through consideration of the displacements of point A:

$$\widehat{xx}_{BA} = \widehat{xx}_{DA} = \widehat{xx}_{HA} = \widehat{xx}_{FA} = Gtb/4h$$

$$\widehat{xx}_{CA} = \widehat{xx}_{GA} = Gtb/2h$$

$$\widehat{xx}_{EA} = \widehat{xx}_{IA} = (EA_{tot}/b - Gtb/2h)$$

$$\widehat{xx}_{AA} = -(2EA_{tot}/b + Gtb/h)$$

$$\widehat{yx}_{BA} = \widehat{yx}_{FA} = Gt/4$$

$$\widehat{yx}_{DA} = \widehat{yx}_{HA} = -Gt/4$$
(5)

$$\widehat{yy}_{BA} = \widehat{yy}_{DA} = \widehat{yy}_{FA} = \widehat{yy}_{HA} = Gth/4b$$

$$\widehat{yy}_{IA} = \widehat{yy}_{EA} = Gth/2b$$

$$\widehat{yy}_{CA} = \widehat{yy}_{GA} = (EA_{tot}/h - Gth/2b)$$

$$\widehat{yy}_{AA} = -(2EA_{tot}/h + Gth/b)$$

$$\widehat{xy}_{BA} = \widehat{xy}_{FA} = Gt/4$$

$$\widehat{xy}_{DA} = \widehat{xy}_{HA} = -Gt/4$$
(6)

Influence coefficients which do not appear in the foregoing equations are equal to zero. It should be noted that the following relations exist between influence coefficients:

$$\widehat{\mathbf{x}}_{\mathbf{M}\mathbf{N}} = \widehat{\mathbf{x}}_{\mathbf{N}\mathbf{M}}$$

$$\widehat{\mathbf{y}}_{\mathbf{M}\mathbf{N}} = \widehat{\mathbf{y}}_{\mathbf{N}\mathbf{M}}$$

$$\widehat{\mathbf{x}}_{\mathbf{M}\mathbf{N}} = \widehat{\mathbf{y}}_{\mathbf{X}_{\mathbf{N}\mathbf{M}}}$$
(7)

These equations follow from Maxwell's reciprocal theorem. They may be easily verified with the aid of the formulas given above.

The operations table and relaxation table are set up in a manner similar to that described in reference 1. The normal stress in a segment of a horizontal or vertical strip between points M and N, and P and Q is, respectively,

$$\sigma_{X} = (u_{N} - u_{M})E/L_{MN}$$

$$\sigma_{Y} = (v_{P} - v_{Q})E/L_{PQ}$$
(8)

APPLICATION OF THE RELAXATION PROCEDURE

TO A MODEL WITH CUT-OUT

The procedure adopted for the calculation of the stress distribution in the reinforced panel with a cut-out was as follows:

First the complete structure (without the cut-out) was balanced. Then the unbalanced forces were determined corresponding to the displacements of the complete structure and to the influence coefficients of the model with the single cut-out. These unbalanced forces were reduced in the third step to negligible quantities through a number of relaxations. The displacement pattern thus obtained was used for a first approximation to the distortions of the model with the double cut-out. The unbalanced forces corresponding to this pattern and to the influence coefficients of the model with the double cut-out were calculated and reduced through relaxations to negligibly small values.

The procedure was found to be rapidly convergent since the cut-outs materially affected the displacements and stresses only in their immediate neighborhood. The double cut-out condition could have been calculated directly from the complete structure, but the intermediate case of the model with the single cut-out was needed for the purpose of comparison with test results.

In figures 6 to 8 schematic drawings of the three model conditions investigated are shown. Table 1 contains the influence coefficients \widehat{yy} , \widehat{xx} , and \widehat{xy} for the model in its three different conditions. The table proper was calculated for the complete model. The first auxiliary table (starred values) gives all those influence coefficients which changed because of the single cut-out. The second auxiliary table contains the influence coefficients the values of which (marked with a dagger) changed when the single cut-out was transformed into the double cut-out. Because of equations (7) only one-half of the total number of the influence coefficients had to be listed.

Table 2 is the Operations Table. It contains individual and block displacements calculated in the same manner as described in reference 1. Several of the boxes in this table contain two figures. The upper figure pertains to the model with the single cut-out; while the lower figure

holds for the model without a cut-out. Where only one value appears in a box, it applies to both conditions of the model.

Since both the model and its loading are symmetric, symmetrically situated points must displace symmetrically. This means that vertical displacements of symmetrically situated points are equal in both magnitude and sense; while their horizontal displacements are equal in magnitude and opposite in sense. Because of these symmetry properties the group operations listed in table 3 are found convenient for the numerical work of relaxation.

In the first line of the Relaxation Table (table 4) the external loads are entered. With the aid of the group operations of table 3 the unbalanced vertical forces are reduced to negligible quantities in comparatively few steps. Details of the procedure followed are not explained here. since they were described in reference 1. However, after these relaxations have been completed, residual forces which are not considered negligible exist in the horizontal direction. The structure must be relaxed, therefore, until the horizontal forces are reduced to negligibly small quantities. Before this is done, however, the total displacement given to each point is obtained and used as a check on previous work (table 5). It may be seen that the residual forces in the check table differ slightly from those obtained before. Since they define the present state of equilibrium more accurately than do the previous residual forces. relaxation should be continued from the values listed in the check table.

Because of the symmetry of model and loading, the horizontal residual forces just obtained are also symmetric. the uppermost horizontal contains the points at which the greatest unbalances occur, the forces there are reduced first. It may be seen that a simultaneous displacement of points A and D toward the axis of symmetry of the model, followed by a similar simultaneous displacement of points B and C. reduces the unbalances considerably (table 6). After these operations have been carried out twice in succession, negligible residual forces remain. Since the unbalances on the other horizontals are of the same nature, steps similar to those just undertaken reduce all remaining unbalances to small quantities. The advantage of reducing the large unbalances of the top horizontal first is almost self-evident. Large unbalanced forces require proportionately large displacements in the relaxation procedure: consequently, forces which are not negligible are thrown on the points of the

NACA TN No. 950

adjacent horizontal when the top horizontal is relaxed. However, when the smaller unbalanced forces of the other horizontals are reduced, the forces transmitted to the top horizontal are negligibly small. As a matter of fact, in the present calculations these forces were fractions of the unit used in the table and were, therefore, not listed.

Since the effect of the relaxations undertaken in table 6 upon the forces in the vertical direction is negligible, no further relaxations are necessary. However, a check is made in order to ascertain the accuracy with which the horizontal relaxations have been performed. The residual forces present before the horizontal relaxations are entered in the top row of the Check Table (table 7). No additional vertical displacements were undertaken after the first check; therefore, a check involving only horizontal displacements suffices. The final vertical and horizontal residual forces are given in the last row of the table. As these forces are negligibly small, the relaxation of the model without a cutout is considered to be completed. With the aid of equations (8) and the total displacements from tables 5 and 7 the stresses in all segments of the verticals and the horizontals may be calculated. The calculations are presented in table 8. It should be noted that $E/L_{MN} = 30 \times 10^6/8 =$ 375 x 104 psi for inch for each segment.

The stresses in the verticals are found to be the same as those obtained in reference 1. This verifies the assumption of reference 1 that the effect of the horizontal displacements upon the stresses in the vertical direction is small in the symmetric model. The stress distribution in the horizontals is given in figure 12.

The problem of the model with the single cut-out now may be attacked. The numerical work is facilitated by the use of the Group Operational Table (table 9) prepared with the aid of table 1. As a first approximation the deflections obtained for the model without a cut-out were assumed to be also the deflections of the model with the single cut-out. The magnitude of the error made can be judged if the unbalanced forces are calculated from these deflections with the aid of the values pertaining to the model with the single cut-out listed in table 2 (Operations Table). These calculations are contained in table 10, which has the title "Check Table of Relaxations for Model without Cut-Out with Operations Pertaining to Model with Single Cut-Out." The forces are in equilibrium at all joints except those in the immediate vicinity of the cut-out, as was to be expected.

Unbalance exists in both the vertical and the horizontal directions at points G, H. L, and M. With this condition as a starting point the model can be readily relaxed.

As before, the unbalanced vertical forces are reduced first. Stringer segment MQ is displaced as a unit (table 11). This step is followed by a displacement of segment DH. The steps are repeated in the same sequence until a state is reached at which individual displacement of the points appear to be advantageous. Finally, a block displacement of stringer IV reduces the vartical residual forces to the magnitudes desired.

The total displacement given to each point is found and is tabulated in table 12. The residual forces obtained in this table now must be considered. They are small in the vertical direction and comparatively large in the horizontal direction. In accordance with the pattern established in reference 1, through suitable operations the unbalanced forces are distributed in such a manner that simultaneous block displacements of the horizontals ABCD and JKLM result in reducing the forces considerably (table 13). A few additional individual displacements followed by a vertical group displacement of the edge stringer DHMQ reduce the unbalanced forces to small quantities. Because the solution of the model with the single cut-out depends on the previous solution of the complete model, a check table which takes into account the total displacements of each point is given in table 14. These displacements are obtained by adding the displacement of each point in table 10 to the displacement of the same point in tables 12 and 13. Since a few of the residual forces are slightly larger than desirable, small adjustments are made in the total displacements of four points. The starred values at the end of the table are the adjusted values of the corresponding starred values in the table proper. At this stage of the procedure the adjustments were found to be the most convenient means of balancing the residual forces. The final residual forces appear in the last line of the table.

In table 15 the stress calculations are presented for the model with the single cut-out. A comparison of the experimental and the calculated normal stress in the stringers is given in figure 9. The dotted lines in figure 12 represent the normal stresses in the horizontals.

With the solution of the problem of the model with the single cut-out now available, the problem of the model with

the double cut-out can be solved in a manner similar to that just described. The Operations Table for Model with Double Out-Out (table 16) is established from the pertinent values of table 1. With this operations table the Check Table of Relaxations for Model with Single Cut-Out with Operations Pertaining to Model with Double Cut-Out (table 17) is calculated from the displacements listed in table 14. The residual forces are entered in the first row of the relaxation table (table 18). A displacement of point G, followed by a rigid body displacement of stringer segment CG, reduces the large unbalanced force at G considerably. Similar operations reduced the force at L. Several individual displacements are then taken, resulting in residual forces which are negligibly small at most of the remaining points also. A rigid body displacement of stringer segment DH is found helpful in this process. The unbalances in the horizontal direction are distributed by displacements of individual points preparatory to a horizontal group displacement of the three upper fields, which in turn reduces the residual forces considerably. A few individual point displacements then suffice to attain unbalanced forces in the horizontal direction which can be considered negligibly small. In this process, however, relatively large vertical forces are introduced at several joints. A group displacement of stringer I, followed by simultaneous displacements of points A, B, N, and O, reduce these remaining forces to small values. The Complete Check Table for Model with Double Cut-Out is presented in table 19 in which the total displacements of the joints are listed as computed from tables 17 and 18. Minor adjustments again are nade in the displacements. They are listed at the end of the table.

The stress calculations are given in table 20. A comparison of the experimental and the calculated direct stress in the stringers is contained in figure 10. The dot-dash lines in figure 12 represent the direct stress in the horizontal strips. The variation of the calculated direct stress in the stringers with the changes made in the original model is shown in figure 11.

In conclusion, it may be stated that, in general, the agreement between calculated and measured stress is reasonably good. In the case of the model with the single cut-out the measured and the calculated stresses almost exactly coincide in the graphs along stringers I, III, and IV. The agreement is almost equally good along stringers II and IV and in the upper portion of stringer III, in the model with the double cut-out. In this model, however, the stress

neasured in stringer I is consistently less than that calculated. The probable reason is an underestination of the load-carrying capacity of the sheet, especially in the upper portion of the nodel. Similarly, the rough assumption of a uniform effective width all over the model might be responsible for the disagreement between experiment and calculation in the neighborhood of the concentrated load applied to the discontinuous stringer.

CONCLUSIONS

In this second report on numerical procedures for the calculation of the stresses in nonoccques tests are described which were carried out at the Polytechnic Institute of Brooklyn in order to establish the stress distribution in sheet and stringer combinations loaded with concentrated loads applied to the stringers. In the first test model there was a cut-out involving one panel of sheet, and in the second model one involving two panels of sheet and the intervening portion of a stringer. The stresses also were determined analytically by a step-by-step approximation procedure. The agreement was reasonably good between the results of the calculations and the experiments.

The suggestions made in the conclusions of the first report (reference 1) regarding details of the numerical procedure again were found to result in a rapid convergence of the calculations. Moreover, it was found that the following approach is advantageous if there is a cut-out in the sheet and stringer combination:

- (1) Calculate the stresses as if the structure were complete (using influence coefficients pertaining to the structure without the cut-out).
- (2) Consider the displacement pattern obtained as a first approximation to the actual displacements of the structure with a cut-out. Determine the unbalanced forces corresponding to these displacements, using the actual values of the influence coefficients in the structure with the cut-out. Reduce these unbalanced forces through a suitable series of relaxations, preferably following the recommendations prosented in the Conclusions of reference 1.

It is believed that this procedure will result in a fairly rapid determination of the stress distribution in

sheet and stringer combinations in which the end points of the reinforcing strips are free to move, provided the cutout is not disproportionately large.

Polytechnic Institute of Brooklyn, Brooklyn, New York, July 1944.

REFERENCES

- 1. Hoff, N. J., Levy, Robert S., and Kempner, Joseph: Numerical Procedures for the Calculation of the Stresses in Honocoques. I - Diffusion of Tensile Stringer Loads in Reinforced Panels. NACA TN No. 934, 1944.
- 2. Cross, Hardy, and Morgan, Newlin Dolbey: Continuous Frames of Reinforced Concrete. John Wiley and Sons. (New York), 1932.
- 3. Southwell, R. V.: Relaxation Methods in Engineering Science. Clarendon Press (Oxford), 1940.

TABLE I. INFLUENCE COEFFICIENTS FOR THE THREE CONDITIONS OF THE MODEL. SHEET 1.

VALUES FOR MODEL WITHOUT CUTOUT.

nm	99 _{nm} x 10 ⁻⁴	x nm x 10 ⁻⁴	nm	99 _{nm} x 10-4	XX _{nm} x 10 ⁻⁴	nm	99 _{nm} x 10-4	xx _{nm}
AB	2.00	46.8	EJ	46.8	2.00	JO	2.00	2.00
Æ	46.8	2.00	EK	2.00	2.00	† KL	4.00	47.8
AF	2.00	2.00	tFG	4.00	47.8	KN	2.00	2.00
BC	2.00	46.8	FJ	2.00	2.00	ко	49.2	4.00
BE	2.00	2.00	tFK	49.2	4.00	KP	2.00	2.00
BF	49.2	4.00	tFL	2.00	2.00	*LM	4.00	47.8
BG	2.00	2.00	*GH	4.00	47.8	LO	2.00	2.00
CD	2.00	46.8	t GK	2.00	2.00	LP	49.2	4.00
CF	2.00	2.00	*+GL	49.2	4.00	LQ	2.00	2.00
CG	49.2	4.00	*GM	2.00	2.00	MP	2.00	2.00
CH	2.00	2.00	*HL	2.00	2.00	MQ	46.8	2.00
DG	2.00	2.00	*HM	46.8	2.00	NO	2.00	46.8
DH	46.8	2.00	JK	4.00	47.8	OP.	2.00	46.8
EF	4.00	47.8	JN	46.8	2.00	PQ	200	46.8
			1				l	

* VALUES FOR SINGLE PANEL CUTOUT.

Р. Э.	2.00 48.I	468 200	GM HL	0	0	HM L'M	47.I 200	0 468	
GL	48.1	2.00	HL	0	0	ĽM	2.00	468	

† VALUES FOR DOUBLE PANEL CUTOUT.

FG	200	46.8	FL	0	0	GL.	0	0
FK	48.1	2.00	GK	0	0	KL	2.00	468

TABLE I. INFLUENCE COEFFICIENTS FOR THE THREE CONDITIONS OF THE MODEL. SHEET 2.

VALUES FOR MODEL WITHOUT CUTOUT.

nm	XU _{nm} x 10 ⁻⁴		nm	XU _{nm} x 10 ⁻⁴	nm	XV _{nm} x 10 ⁻⁴		nm	XU _{nm} x IO-4		nm	XU _{nm}		nm	XU _{nm}
AB	2.00		ВА	-2.00	EJ	-2.00		JE	2.00		JO.	2,00		01	2.00
AE	-2.00		EA	2.00	EK	2.00		KE	2.00		t KL	0		+ LK	0
AF	2.00		FA	2.00	† FG	0		t GF	0		KN	-2.00		NK	-2.00
ВС	2.00		СВ	-200	FJ	-2.00		JF	-2.00		KO	0		OK	0
BE	-2.00		EB	-200	† FK	0		† KF	0	П	KP	2.00		PK	2.00
BF	0	1	FB	0	+FL	2.00	Ш	tLF	2.00		*LM	0	l	*ML	0
BG	2.00	ĺ	GB	2.00	* GH	0	П	*HG	0	l	LO	-200	l	OL	-2.00
CD	2.00		DC	-2.00	t GK	-200		†KG	-2.00		LP	0		PL	0
CF	-2.00		FC	-2.00	#1GL	0		*ILG	0		LQ	2.00		QL	2.00
င		۱	GC	0	*GM	2.00	П	*MG	2.00		MP	-2.00		PM	-200
СН	2.00		НС	2.00	*HL	-2.00		*LH	-2.00		MQ	2.00	l	QM	-2.00
DG	-2.00		GD	-2.00	*HM	2.00	11	*MH	-2.00		NO	-2.00		ON	2.00
DH	2.00		HD	-2.00	JK	0	$\ \ $	KJ	0		OP	-2.00		PO	2.00
EF	0		FE	0	JN	-200		NJ	2.00		PQ	-200	ł	QP	2.00
						}							l		

* VALUES FOR SINGLE PANEL CUTOUT.

	GH	-2.00 0	HG	2.00	GL	2.00	LG	-200	GM	0	MG	0	
-	HL	0	LH	0	HM	0	МН	0	LM	2.00	ML	-2.00	

† VALUES FOR DOUBLE PANEL CUTOUT.

FG	-2.00	GF	2.00	FK	2.00	KF	-2.00	FL	0	LF	0	
GK		KG	0	/GL	0	الد		KL	2.00	LK	-2.00	
		L		L		L		<u> </u>		l L	<u> </u>	-

TABLE 2. OPERATIONS TABLE FOR MODEL WITHOUT CUTOUT AND WITH SINGLE CUTOUT. SHEET I.

(WHERE TWO FIGURES APPEAR IN A BOX, THE LOWER PERTAINS TO THE FORMER CONDITION, THE UPPER TO THE LATTER CONDITION.)

DISPL	Y	YB	Y _c	YD	¥	YF	YG	YH	YJ	Yĸ	Ϋ́	ሂ _ብ	YN	Υ ₀	Yp	YQ	X	X _β	Х _С	X _D	Xε	Χ _F	X _G	ΧH	ΧJ	X _K	Χ	X,	Χ _N	X _o	χ ρ	Χo
	5 <u>0</u> 6				46.8						_							200			200											\Box
V _E - 1	16.8	200			01.6	4.00			46.8	2.00							200	2.90			0	0	•	-	2.00	200						П
V _J - 1					468	2,00		_	101.6	4,00			46.8	2,00							2.00	200			0	0			2,00	200		П
V _N - i									46.5	200			520	2.00											Z <u>0</u> 0	<u> 200</u>			Z.00	200		П
VBLOCK - I	4.00	4.64	Γ		880	800			8	800			460	4,00			<u> </u>	48			0	٥			0	0			400	4,00		
V _B = 1	2.00	5/2	200		2,00	45.2	2,60					·					Z.00	0	<u> 200</u>		2 <u>20</u>	0	200									
V _F - 1	200	492	2.00		4.00	14.4	490		2.00	49.2	2.00						200	0	200		0	0	_		욂	0	2.00					
V _K I					2.00	49.2	200		4,00	些	400		200	492	2.00						2.00	0	Z 60		0	0	0		2 <u>0</u> 0	0	2.00	
V ₀ -!									200	492	2.00		2.00	572	2.00										200	0	200		2 <u>8</u> 0	0	200	
V _{BLOCK} = 1	100	휧	400		00,8	<u> 1770</u>	8		0.00	3	890		4.00	<u>avo</u>	130		3	0	3		0	0	0		0	0	0		400	0.	400	
V _C = 1		200	57.2	200		2,00												200	0	230		200		200								
V _G -1		28	49.2	2.00		4.00	弘业	2.00 4.00		2.00	福祉	2.00						200	0	280		٥	80	0								
V I						2.00	48.1 49.2	့ ရှိ		4.00	なな	200 400		2.00	452	200						윱	80	0 29		0	럞	<u> 5</u>		8	٥	200
V _p - 1										200	49.2	290		200	<u>57,2</u>	2.00										2,00	ı.	200	L	퉝	0	2.00
V _{BLOCK} = I		4,60	8 <u>8</u>	4.00		B.00	흴뎧	4.00 8.00		9.00	39	38		400	8.00	4,00		8	•	460		0	80	& 0	,	0	4.00	480		<u> 400</u>	0	4.00
V _D = 1			2.00	<u>50</u> 8			28	46.8											20	200				8								
V _H - 1			2.00	46.8			88	OL6			200								200	200				홟°			200	200				
V _M = 1	П							47:1 46.B			266 4.00	꼾			2.00	46.8							200	0 2.00			2.00 O	200			2,00	500
V _Q = 1											3	46.8			2.00	<u>50.8</u>											Z.00					2.00
V _{BLOCK} -I			400	400			4.00 8.00	88			4.00 8.40	381			4.00	셷			400	440			380	4 <u>8</u> 10			4.00	4,60 0			100	4.00

UNDERLINED NUMBERS ARE NEGATIVE. FORCES IN LB., DISPLACEMENTS IN IN. X 10⁻⁴.

TABLE 2.. OPERATIONS TABLE FOR MODEL WITHOUT CUTOUT AND WITH SINGLE CUTOUT. SHEET 2.

(WHERE TWO FIGURES APPEAR IN A BOX, THE LOWER PERTAINS TO THE FORMER CONDITION, THE UPPER TO THE LATTER CONDITION)

DISPL.	Y	YB	Yc	YD	YE	YF	YG	Y _H	Ϋ́	YK	Y	Y,	ሂ	8	Ϋ́	γ	X	Хв	X _C	X_D	XE	X _F	X _G	X _H	X,	X _K	ΧL	X,	X _N	X _o	ኢ	Ko
U _A — i	200	200			200	200							┪				<u>27</u> 2	44.8		<u> </u>	2.00	200										
	200	0	2.00		200	0	2.00						▎				46.8	<u>01</u> 6	44.8		2,00	490	200									
u _c = i		3	0	200		250	0	200										46.B	2	468		200	4.00	Z,00			Γ					
u _p = 1			3	Z.00			鎬	2,00												50,8	I			2,00								
U _{BLOCK} = I	430	0	0	190	400	0	0	4.00										18	욂	100	20	800	800	250								
U _E - 1	2.00	18			0	٥			8	26.							2.00	200			55.8	47.8			2,04	200						
	2.00				i	٥	1		81		2.90							8	· .	I	478	_	L			4,90						
u _c - I		8		2.00			2.00 O				200							8	480	500		47.8	驺	47.0		2,00	2.06 4.00	٠\$				
u _н = 1				2,09			200 O	30			200	-81							Ι΄.	200	1		33	읦			200	2.00				
U _{BLOCK} -1	£00	٥	0	4.00	0		A 00	80	8	0	4.00						400	8,00	8	4.00	18	3	홟					4.00				
u _j = 1		_	Ц		2.00				٥			_		200							240				ı	47.8	L			8		
u _K = 1					260				0	ł	0		200		200				_	L	280						L		1. 1	4,00		$oldsymbol{L}$
U _L = 1		L		<u> </u>	匚	290	*	26	_	0	뺭	200		200	_	2.00						200	88	0 8	L.	47.8	亞				_	2.00
U _M = 1					<u> </u>		08	<u> </u>		_	8	200	L		28					L.				200							8	11
UBLOCK - I					4.69	_	30	400	0	0	P. P.				٥	2	Щ			_	4.00	8	28	Ī	_		_	88	_	_		400
U _N = 1									2.00					200			Ц			<u> </u>						200		_		3		Ш
u _o - 1									2,00		죍		8	ŀ	81											400				ᆁ		
U _p = 1											0	_	_	_	0					L							_	3	-		\equiv	46.8
u _o = 1				L							2.00	ĺ		<u>. </u>	200	ĺ								L				200		_		50.8
U _{BLOCK} = 1									4.00	0	0	F00	400	0	0	400	Ш						<u></u>		4.00	8.00	8.00	4,80	3	<u> </u>	<u> </u>	400

UNDERLINED NUMBERS ARE NEGATIVE. FORCES IN LB., DISPLACEMENTS IN IN. X 10-4.

TABLE 3. GROUP OPERATIONS TABLE FOR MODEL WITHOUT CUTOUT

DISPL.	YA	YB	Y _c	Y_D	YE	YF	Ϋ́ς	Y _H	Ϋ́J	Yĸ	۲	Y,	Y _N	Yo	Y _P	YQ	X _A	Хв	X _C	Χ _ο	Χ _E	Χ _F	X _G	X _H	Χ,	Xĸ	ΧĹ	X	X	χ _ο	ኢ _ዮ	X _Q
V _A - V _D - I	50.8	2.00	200	52.0	468	Z.00	200	468									<u> 28</u>	2.00	200	200	200	250	욃	500								\Box
V _J -V _M -1					46.8	200	2.00	16.8	퀽	400	4.00	鍧	468	200	2.00	46.8					200	2 <u>.00</u>	8	2.00					260	20	2.00	200
VN=VQ=1									468	2.00	200	3	췲	200	200	<u>50.8</u>									욃	220	2.00	28	200	28	500	2,00
V _B -V _C -1	290	5 <u>5</u> 2	5 <u>5</u> 2	200	200	51.2	5L2	2.00									200	200	<u> 220</u>	죎	200	2.00	200	2.00								Ш
VK-AF-1					200	52	27.5	2.00	욯	뉡	10.4	40	200	51.2.	51.2	200					200	200	200	2.00					2 <u>00</u>	2 <u>00</u>	2.00	200
Vo-Vp-I									200	51,2	51.2	2.90	200	5 <u>5.</u> 2	552	200				L	L_				200	2.00	200	2,00	2 <u>00</u>	200	200	200
U _B -U _C -I	翁	290	200	200	28	200	200	2.00									46.8	48.4	48.	3	200	200	2 <u>8</u> 2	200								
U _A U ₀ -1	<u>20</u> 0	200	200	2,00	200	200	2.00	2.00									50.8	46.B	4.8	50.8	2,00	2.00	2.00	2 <u>,00</u>							L	\sqcup
U _E =-U _H -1	2.00	200	28 0	2,00					즮	8	200	2 <u>.0</u> 0					2.00	2.00	2 <u>00</u>	옼	5 <u>5.</u> 6	178	47.8	53,8	2,00	2.00	500	200		L	L	Ш
U _F U _G -1	200	<u> 20</u> 0	<u>23</u> 0	200					<u> 28</u>	260	2,00	2 <u>00</u>					200	2.00	200	됢	47.8	594	59.4	<u>478</u>	2,00	2.00	2.00	500			L	Ш
U _J =−U _M =1					2.00	<u>200</u>	500	2.00					2 <u>0</u> 0	2.00	2.00	2.00					2,00	2.00	<u>57</u> 0	200	5 <u>5.</u> 8	47.8	17.8	55.0	2.00	200	2.00	2.00
U _K "-U _L "1					200	200	200	200					2 <u>00</u>	200	2.00	200					2.00	200	200	200	47.8	<u>53.4</u>	159.4	17.8	200	200	200	2 <u>0</u> 0
UN=-UQ= 1									200	200	280	200	200	2.00	<u> 100</u>	2.00							L		200	200	2.00	200	50.8	16,0	46.8	50.8
U ₀ =-U _p =1									500	500	500	2,00	200	500	200	2.00									2.00	200	200	200	46,8	42∕	48/	468
VAEJN" VDHMQ" I	4.60	4.00	400	4 <u>0</u> 0	200	8.00	5,00	8200	e20	00.0	800	g <u>00</u> 0	400	4,00	400	489	420	400	4.00	4.00									100	400	100	400

UNDERLINED NUMBERS ARE NEGATIVE, FORCES IN LB., DISPLACEMENTS IN IN. X 10-4.

TABLE 4. RELAXATION OF VERTICAL FORCES FOR MODEL WITHOUT CUTOUT.

			Yc	YD	YE	YF	Y _C	ሂ	Υ,	YK	Ł	Y _M	YN	8	Y p	Yo	X,	XΒ	Xc	X ₀	XE	XF	Χ _G	Xμ	XJ	Xĸ	X.	X,	X _N	χ _ο	Χ ρ	Χq
EXTERNAL LOADS				120									\$	60	60	60																
VA-VD =-24	Ю	-4					- 4	7									4	4	-4	- 4	- 4	-4	4	4		Γ-	<u> </u>		Γ-		_	
		-4	-4	-10		-4	-4	Š									4	4	-4	-4	1 7	4	A	4	Γ		Г	Г				
VJ-VM-173	Ь.,	_		Ц,	3	_3	3		176			176				81		<u> </u>	L_	L	-3	-3	3	3	L		_	<u> </u>	3		- 3	-3
VN = VQ = 338					2	-1	-\	-20	176 156	7	ľ	176 156			63 7	141					-7	-7	7	7	-7	_ 7	٦	7	3	3 7		-3 -7
Va-Vc25	-1	14	14		1	-13	-13		-20	14	14	- 20	-26	70	70	-28		-1					, T	-1	-7	-7	7	7	10	10	-10	10
				-11							_				-	\vdash	3			-3	-6	-6	6	6	-		-	-			-	-
VK- √r - '96		Щ	_	<u> </u>			34			-73					34						ŀ	l	-1	-1					-1	-1	_ 1	1
Vo+Vp=1.54					-20	20	20	Ŗ	1 7	3 3				194 -85							-5	Ą.	5	5	3	3	-3	-3	-3	-3	-9 3	, 9
VAEJN - VDHMQ25	Ю	-10	\$	20	20	-20	20		14 20	20 20	29 28	14 20		19 29			10	10	-10	-10					-4	-4	4	4	-10	-6 -10	-6 10	-6
VJ-VM04	-		٥		٥ -2	0	0	0 -2	6			6	-14 -2	9	9	14 -2	13	13	-13	-13	-5	-5	5	5	-4	-4	4	4	4	-4		4
V _N - V _O 25					-2				N-12	-1	-1	10 12	-16 13	-1	-1	16 13											7		-	-1		1
V8-VC02		-	1				_1	0	-2	-	-1	-2	-3	8	8	-3									-3	-3	3	3	-5	-5	5	5
V _K V _L 06		1	1			7	~1 3	-2		-7	-7			3						П					_							
						2	_			-8	-8			11	11					\vdash								\vdash	$\vdash \downarrow$			
Vo-Vp20				H		_				9	1 5			7	41		Щ		-	Щ			_			Щ	\vdash					
VAEJN - VOHMQ25	1	-1	-1	ı	Z	-2	-2	7.	2	2 -2	2 2	Z	1	0 -T	0. T	1	1	ı	-1	-4									~1	-l	ı	ŧ
RESIDUAL	0	0	0	0	0	0	0	0	0	0	0	0	-2	1	-1	-2	14	14	14	14	-5	-5	5	5	- 3	-3	3	3	-6	-6	6	6

TABLE 5. CHECK OF RELAXATIONS IN TABLE 4.

DISPL.	YA	YB	Yc	YD	YE	Y _F	Yc	Y _H	Υ _J	Yĸ	Ϋ́L	<mark>ሂ</mark>	ኢ	Υ ₀	Yp	Υ _ο	X _A	X _B	X _c	X _D	Χ _E	X _F	Χ _G	X _H	ΧJ	Xĸ	X.	X,	X,	X _o	Χ _P	Χ _Q
EXTERNAL LOADS	-12.0			120									60	60	60	60											ſ		_			
VA=VD=-4.91	250	-10	-10	250	230	-ю	40	230									ю	10	-10	-10	-10	-10	10	10	Г						\Box	
V _B *V _C *27	-1	15	15	-1	-1	-14	-14	-1			Γ				Г		-1	-1	١	١	1	١	-1	-1								
VE"VH"-2.75	129	-6	-6	-129	280	-11	41	280	129	-6	-6	-129		Г			6	6	-6	-6					-6	-6	6	6			П	
V _F -V _G - 0																					Γ						Г				П	
V _J =V _M =-1.06					-50	, 2	-2	-50	108	-4	-4	108	-50	-2	-2	-50				Г	2	2	-2	-2					-2	-2	2	2
V _K =V _L = .72					_	37	37	1	3	-79	-79	3	ī	37	37	-					1	1	-1	-1					-1	-1	1	T
VN-VQ33								Г	15	I	ı	15	-17	1	٦	-17							П		-1	-1	ī	1	-	ī	-1	– Í
$V_0 = V_P = 1.74$									3	89	89	3	3	-96	-96	3									3	3	-3	-3	-3	-3	3	3
RESIDUAL	0	-1	-1	0	0	0	0	0	O	١	1	٥	-3	0	0	-3	15	15	-15	-15	-6	-6	6	6	-4	-4	4	4	-5	-5	5	5

TABLE 6. RELAXATION OF HORIZONTAL FORCES FOR MODEL WITHOUT CUTOUT.

DISPL.	YA	YB	Y _c	ሃ _D	YE	Y _F	Y_G	Ϋ́	۲ _J	Υĸ	YL	<mark>ኒ</mark>	Y _N	Yo	Yp	YQ	XA	XB	X_{c}	$X_{\!\scriptscriptstyle \mathrm{D}}$	Χ _E	X _F	X _c	X _H	X,	Xĸ	ΧL	X,	Χ _N	X _o	Х _Р	X _Q
RESIDUAL FORCES	0			0							١	٥			0	-3			j		-6	-6	6	6	-4	-4	4	4	-5	-5	5	5
UAUD =.30	-1	T	ī	-1	-1	1	1	-1									-15	7	-14			1	-1	-1			,					•
u _g -u _c 20	-1	٥	٥	-1	1	1		-1									09	29 -29	-29 29	9		-5	5	5								
u, -u _o 18											l I						9 -9	08	0 -8	-9 9							L					
ug-u _c =.05	Г																0 2	8 -8	8 8													
Ug-UH-09	i																2	0	0	-2	5	-4	4	-5								
u _r u _c 06																					0 -3		-9	_								
uu _M =::07																					-3	0	0	3	4	-3	3	-4				
u _K =-u _L =04																									0 2-	-7 6	7 -6	0 2				
U _N =-U _O =- 10										-															-2	Ť	. 1	2	5	-5	5	-5
u ₆ -u _p 07																								•					0 3		10 -10	
RESIDUAL	-1	0	0	-1	-1	1	١	-1	0	i	١	0	-3	0	0	-3	2	0	0	-2	-3	0	0	3	-2	-1	1	2	-3	0	0	3

TABLE 7. CHECK OF RELAXATIONS IN TABLE 6.

DISPL.	Y	ሂ	Y _C	Y _D	YE	Y _F	Y _G	Y _H	Y	Yĸ	ሂ	Ϋ́м	YN	Yo	Yp	YQ	X	X _B	X _C	X _D		X _F	Χ _G	· .	\sim	Xĸ	ኢ	XM		X _o	Χ _P	Xq
RESIDUAL. FORCES	o	-1	1	0	٥	0	0	0	0	ľ	ı	٥	-3	0	0	-3	15	15	-15	-15	-6	-6	6	6	-4	-4	4	4	-5	-5	5	5
u _A u _D 48	-1	-	ī	-1	-1	ı	I	-1									-24	22	-22	24	1	ı	-1	-1								Ш
u ₈ -u _c 25		1	ī	-1	-1	ī	ı	-1									12	-37	37	-12	١	1	-	7								
u _e u _H 09																					5	-4	4	-5								
uu06																					-3	Ю	-10	3								
uu07																									4	-3	3	-4				
U _K U _L 04	_																			Γ					-2	6	-6	2				
U, - U - 10																													5	-5	5	-5
u ₀ -u _P 07																													-3	10	-10	3
RESIDUAL	-2	ı	١	-2	-2	2	2	-2	Ó	١	١	0	-3	0	0	-3	3	0	0	-3	-2	2	-2	2	-2	-1		2	-3	0	0	3

TABLE 8. STRESS CALCULATIONS FOR MODEL WITHOUT CUTOUT.

CALCULATION OF STRESSES IN VERTICAL STRINGERS.

MEM	IBER N	Vm TOTXIO	V _{n tot} xio ⁴	(V _{n тот} - V _{m тот})10 ⁴	K x 10-4 LB. IN.2/IN.	STRESS PSI.
AE	DН	- 4.91	- 2.75	2.16	375	810
EJ	нм	- 2.75	- 1.06	1.69	я	634
JN	MQ	- 1.06	.33	1.39	ŧŧ	521
BF	CG	27	0	.27	10	101
FK	GL	ο	.72	.72	11	270
ко	LP	.72	1.74	1.02		382
L						

CALCULATION OF STRESSES IN HORIZONTAL STRIPS.

MEMBER M n	U _{M TOT} XIO ⁴	u _{n тот} хю ⁴ ін.	(u _{п тот} и _{ттот})ю ⁴	K x 10 ⁻⁴ LB./in	STRESS PSI.
AB CD	.48	.25	23	375	- 86
BC.	25	25 ·	50	11	-187
EF GH	09	06	.03		11
FG	06	.06	.12	11	45
JK LM	07	04	.03	10	[1
KL	04	.04	.08	N	30
NO PQ	10	07	.03	H	11
OP	07	.07	.14	11	53
-	<u> </u>				

TABLE 9, GROUP OPERATIONS TABLE FOR MODEL WITH SINGLE CUTOUT.

DISPL.	Y,	YB	Yc	Y_D	YE	YF	Y _G	Y ₄	Ϋ́	Yĸ	ሂ	<mark>ኒ</mark>	YN	Υ ₀	Ϋ́Р	40	X,	Хв	Xc	X _D	ΧĘ	XF	Χ _G	X _H	ΧJ	Xĸ	X _L	Хм	X _N	Χo	Χρ	Χo
UFUGI	2.00	500	200	2.00			200	0Q.S	7.00	200	0	۵					200	200	200	2,00	478	524	54.4	<u>46</u> 8	200	200	0	0				
U _K U _L -1					200	200	0	0			2.00	2.00	200	200	200	200					2,00	2,90	0	0	47,8	534	1544	4 <u>6.</u> 8	2,00	2,00	2.00	200
V _{DHMQ} =			400	4 <u>00</u>			4,00	4.00			4.00	4.00			8	8			400	400			多	4.60			400	4.00			400	4 <u>.00</u>
V _{CGLP} = I		400	8.00	4,00		6,00	БÖ	400		S	엻	400		420	80	ş		400	0	4.00		0	20	4,00		0	400	4.00		4.00	0	400
V _M -V _Q -1								47.1			8	51			8	48											400	400			욁	4.00
VVH-1			4.00	8			400	51.1				47.1							3	400			18	100					ļ			\prod
u _c -u _H -I		Z00	200	1 20			4,00	420		<u> 20</u> 0	200	0						200	680	490		47.8	<u> 11</u> 8	7 00		200	200	0				П
U _G U _H -1		2.00	2 <u>20</u>	0			0	0		2,00	2.00							Z9 0	200	0		47.B	5	37. 6		200	2.00					
u _F -u _G -I	2.00	260	230	200			200	2.00	2.00	220	400						280	6,00	600	2.00	47.8	6 <u>3.8</u>	58.8	468	200	P00	400					$ \Box $
UEUHI	2.00	2	200	2.00			2.00	2,00	200	2.00							200	2.00	200	200	558	47,8	458	50.8	200	200	Γ					
U,U, i				i	200	200					2.00	2 <u>9</u> 0	2.00	200	200	200					2.00	200			5 <u>5.</u> 8	47.8	468	50.8	2.00	2,00	200	2.00
I VDCD	400			4.00	0		420	400			400	400	4.00			4.90	4.00	800	820	400	<u>1.00</u>	690	200	4.00	8.00	16.00	200	400	400	8 <u>0</u> 0	8,00	100
UJKLM "-1		Ĺ	Ĺ	<u>.</u>				L		L		<u> </u>				L												L	L			

UNDERLINED NUMBERS , ARE NEGATIVE. FORCES IN LB., DISPLACEMENTS IN IN. X 10-4.

TABLE 10. CHECK TABLE OF RELAXATIONS FOR MODEL WITHOUT CUTOUT WITH OPERATIONS PERTAINING TO MODEL WITH SINGLE CUTOUT.

				_										_					_	_	_							_				
DISPL.	YA	YB	Yc	Ϋ́D	YE	YF	YG	YH	Yی	Yĸ	ሂ	Y _M	> 2	Yo	YP	YQ	XA	XΒ	X_{C}	X_D	XE	X_{F}	Χ _G	XH	ΧJ	XK	X.	X_M	Χ _N	Χر	X_{P}	XQ
EXTERNAL LOADS	-120			120									60	60	છ	60																
V _A = V _D =~4.9I	g	-10	-10	250	-230	-10	-10	-230									Ю	10	-10	40	-ю	-10	8	10								
V _B - V _C 27													•				-1	-1	1	1	1	-	-1	~1								\Box
V _E = V _H -2.75	129	-6	-6	129	280	-11	-6	269	129	-6	0	-130					6	6	-6	-6			6	6	-6	-6						
V _F = V _G = 0																											••					
V_= V1.06					-50	-2	0	-50	108	-4	-2	104	-50	-2	-2	-50					2	2					-2	-2	-2	-2	2	2
V _K - V _L 72					1	37	36	0	3	-79	-76	1	١	37	37	-					1	1					-1	-1	7	-1	ī	ī
VN = V0 = .33							<u> </u>		15	1	1	15	-17	1	1	-17								<u> </u>	-1	-1	١	١	1	1	-1	-
Vo= Vp= 174						Г			3	89	89	3	3	-96	96	3								_	3	3	-3	-3	-3	-3	3	3
U, -UD48	-1	1	1	-1	-1	1	ľ	-1									-24	22	-22	24	١	. 1	-1	-1								
U _B "-U _C " .25	7	١	1	-1	-1	١	1	4									12	-37	37	-12	١	1	-1	-1								
U _E -U _H 09																					5	-4	4	-5								
uu06							<u> </u>														-3	10	-9	3								
น ร -น ร 07						Г																			4	-3	3	-4				
U _k -U _c 04																				Γ					-2	6	4	2				\Box
UU10				Γ																									5	-5	5	-5
Ug-Ug07					Γ																								-3	10	40	3.
RESIDUAL	-2	١	١	-2	-2	2	8	-14	0	Ī	12	-7	-3	٥	0	-3	3	0	0	-3	-2	2	8	11	-2	-1	-8	-7	-3	0	0	3

TABLE II. RELAXATION OF RESIDUAL VERTICAL FORCES FOR MODEL WITH SINGLE CUTOUT.

DISPL.	YA	YB	Yc	YD	YE	YF	YG	环	ΥJ	YK	YL	Y _M	¥	Yo	Ϋ́ρ	مح	X	XΒ	Xc	X_D	ΧE	ኢ _F	Χ _G	X,	ΧJ	XK	ΧĹ	X,	X,	X _o	X_{P}	χo
RESIDUAL FORCES	-2	١	١	-2	-2	2	8	-14	٥	٦	12.	-7	-3	0	0	-3	3	0	0	-3	-2	2	8	11	-2	-1	-8	-7	-3	0	0	3
VM- VQ14								-7			-	7			-	Ī											-1	-1		 ~	-	T
V _D = V _H =-,41			-2	2	,		-2	-21 21			Ξ	0 9			7	-2			-2	N			2	2			-9	-8				4
V _M = V _Q =-37			-1	0			6	0 77			7	99			7	-			-2	157			2	13			-,	-1			1	١
V _D = V _H =33			-	ı			7	77.7			10	фo			-2	-1			-1	7			١	•			-10	-9			2	5
V, - V31			-2	١			5	0 -15			-1	16			7				-3	-6			11	14			-1	-1			_	1
V _D - V _H 29			-1	١			7	15 15			9	94			-3	0			-1	-1			-	_			71	-10			3	6
V _M V _q .27			-3	2			4	0 -13			-1	-14 14			-	1			-4	-7			12	15			-	7			1	1
V _H =13				-6				-13 13			8	-6			4	-											12	-11			4	7
V _M =-,06				-4				0 -3				96				-3																
V _L 07							3	-3			-8	0			3	-2																
v _c 06			3				7-7				0				-1																	
80av			0	4			0	-4			3	,																				
V _H = −.07				0 -3				-7 7				-3																				
V _{DHMQ} 5			-2	-შ 2			-2	0 2			-2	-3 2			-2	2			-2	-2			2	2			-2	-2			2	2
RESIDUAL	-2	١	-2	-1	-2	2	-2	2	0	١	١	-1	-3	0	-3	0	3	0	-6	-9	-2	2	14	17	-2	-1	-14	-13	-3	0	6	9

TABLE 12. CHECK OF RELAXATIONS IN TABLE 11.

DISPL.	Ϋ́A	YB	Yc	Ϋ́	YE	YF	Y _G	Ϋ́́н	۲ _J	YK	۲L	Y <u>×</u>	Ϋ́	Yo	Ϋ́	Yo	X _A	Хв	X _C	X_D	ΧĘ	X _F	X _G	XH	XJ	Xĸ	ΧĹ	Xγ	Χ _N	Χo	ኢ _ኮ	X_Q
RESIDUAL FORCES	-2	١	١	-2	-2	2	8	-14	0	١	12	-7	တု	0	0	-3	ีก	٥	٥	-3	-2	2	8	11	-2	-l	-8	-7	-3	G	0	3
V _D = - 1.61			-3	82			-3	-75									!		-3	-3			3	3						-		
V _H =-1.73			-3	-81			-3	169				-81							-3	-3			3	3								
V _M =-1.65						Γ		-78			-3	162			-3	-77											-3	-3			3	3
V _g =-1.59											-3	-75			-3	81				Г							-3	-3			3	3
V _c - 0																																•
V _G = :06			3				-7				3																					
V _L 07							3				-8				3																	
RESIDUAL	-2	1	-2	-1	-2	2	-2	2	0	Ī	ī	-1	-3	0	-3	1	3	0	-6	-9	-2	2	14	17	-2	-1	-14	-13	-3	0	6	9

TABLE 13. RELAXATION OF RESIDUAL HORIZONTAL FORCES FOR MODEL WITH SINGLE CUTOUT. SHEET 1.

	YA		Yc	፟	YE	YF	Ϋ́c	¥	Ϋ́J	YK	YL	Y _M	γŽ	Yo	Yp	YQ	X,	Χ _B	X	X ₀	ΧĘ	XF	Χ _G	X,	X,	Χĸ	ΧĹ	×	Χ×	X _o	Х _Р	Xq
RESIDUAL FORCES	-2	l	-2	-1	-2	2	-2	2	0	1	-	-1	-3	0	t i	١	3	0	4	-9	-2	2	14	17	-2	-1	-14	73	-3	0	6	9
$U_0 =10$																			-5													
u _B = .06																	3	-6	-11 3	-4												
u _H = .26			١	-1			-	-1						-			6	-6	-8	1			12	-13								
u _F =29	-1		7-	-2			-1	-	1		-1						-	-1	-7 -1	-3	-14	32	84	4	-1	-1	-1					
u _E =38	-3 -1	1	0						1	I	0						5	-7 -1	-8		-16 21	34 -18	12		-3 -	-2 -1	-15					
U _M =18	-4	2							2	0							4	-8			5	16			-4	-3	-8	9				
u _K = .23																						_			11	-26	-23 11	-4		1		
u, = .27					,	-1							-	1							١	17			7 15	-29 13	12		١			
u _o 10					-1	1							-4	1							6	18		-	-8	76			-2	2	5	-5
u _o =06																													-3	6	11 -3	4
U _{ABCD} = U _{JKLM}	4			-4			4	-4			4	-4	4			-4	4	8	8	4	- 6	-16	-12	-#	8	њ	12		-5 -4		გ -8	-4
RESIDUAL	0	2	0	-6	-1	T	3	-3	2	0	4	-5	0	1	-3	-3	8	0	0	1	-2	2	0	0	0	0	0	0	-9	0	0	0

TABLE 13. RELAXATION OF RESIDUAL HORIZONTAL FORCES FOR MODEL WITH SINGLE CUTOUT. SHEET 2.

DISPL.	Y,	YB	Yc	YD	YE	YF	YG	4	Y	YK	Y	Y _M	Y 2	Yo	Yp	Yo	XA	ΧB	Xc	Xo	XE	XF	XG	X,	χ _J	Xĸ	×	X,	X,	X _o	Χp	X _c
RESIDUAL FORCES	٥	2	0	-6	-1	ī	3	-3	2	0	4	-5	0	,	-3	-3	8	0	0	. 1	-2	2	0	0	0	0	0	0	-9	\vdash	-	H
UA = .12																	-6	6				<u></u>	┝┈	_		┝		\vdash	├-		 -	
u _c =06																	2	-3	6	-3												T
u _p 09															•			3	6-4	-2 5												T
U _M 14																			2	3									7	-7		
U _p 09																													-2	-7 4	-9	4
El. – ¿U				,					•													· · · · · ·								-3	-9 6	
V _{DHNO} -5			-2	2			-2	2			-2	2			-2	2			-2	-2			2	. 2			-2	-2			-3 2	-3 2
RESIDUAL	0	2	-2	4	T	Î	-	-1	2	0	2	-3	1	0	-5	-1	2	3	0	1	-2	2	2	2	0	0		_	-2	-3	-1	-1

TABLE 14. COMPLETE CHECK TABLE FOR MODEL WITH SINGLE CUTOUT.

* ADJUSTED VALUES APPEAR AT END OF TABLE. SHEET I.

DISPL.	YA	Y _B	Yc	Y_D	YE	Y _F	Ϋ́G	¥	Υ _J	Yĸ	YL	YΜ	Y _N	Yo	Yp	YQ	X _A	Хв	Χ _c	Χ _D	Χ _E	X _F	Χ _G	ΧH	ΧJ	Xĸ	ΧL	XΜ	X _N	X _o	Хр	XQ
EXTERNAL LOADS	120			-120									60	.8	60	60																
V _A =-4.91	250	-10			-230	-10											10	10			-10	-10										
V _E =-2.75	129	-6			279	-11			129	-6			į				6	6							-6	-6						
0.1−−ر∨					-50	-2			108	-4			-50	-2							2	2			_				-2	-2		
V _N = .33									15	1			-17	1											-1	7			1	1		
V _B =27	-1	15	-1		-1	-13	-1										-1	-	1		-		-1									
V _F - 0	Γ																						-									
V _K = .72					1	35	1		3	-82	3			35	_						1		-1						-1		1	
V ₀ = 1.74									ო	86	3		3	100	3										3		-3		-3		3	
V _c =-,27		7	15	-1		7	-13	-1										-1		1		١		-1						Ш		
V _G 06			3				-7	L			.3																L			Ш		
V _L 79						2	38			3	-86	2		2	39	2						٠ 2	2				-2	-2		-2		2
* Vp = 1.74										3	86	3		3	-100	3						·				3		-3		-3		3
* V _D =-7.02			-14	357			-14	-329											*	14			14	14								
V _H =~4.98			-10	23 3			-10	488				-235							-10	-10			10	10			Ĺ					
V _M =-3.21			L.					1 51			-6	34			-6	150									<u> </u>		-6	-6		Ш	.6	6
V _Q =-1.76											-4	-82			-4	89		<u> </u>		_							-4	-4		Ш	4	4
U _A =40	I	-1			1	-1											20	-19			-1	7										
U _B =69	I		-1		١		-1										-32	_	-32	_	-1	_										
U _c =-1.31		3		-3		3		-3										-61	133	-61		-3	- 5	-3	L		L.					
U _D =−1.67			3	-3			3	-3											-78	85			-3	-3								

TABLE 14. COMPLETE CHECK TABLE FOR MODEL WITH SINGLE CUTOUT.

* ADJUSTED VALUES APPEAR AT END OF TABLE. SHEET 2.

DISPL.	YA	YB	Yc	YD	YE	YF	Y _G	YH,	YJ	Yĸ	YL	Υ _Μ	Yz	Yo	Ϋ́P	Ϋ́	X _A	Х _В	X_{C}	X _D	ΧE	X _F	X_{C}	Χ _H	ΧJ	Xĸ	ΧĹ	X _M	X _N	X _o	Χ _Ρ	XQ
UE47	-1	1							1	-1							7	7			26	-22			-1	-1						
U _F =35	-1		1						ı,		-1						7	Ŧ	7		-17	39	-1 7		7	-1	1					
*U _G = .06																				Ĺ		3	-6	3		L						
U _H = .35			l	-1		1	-	-1											1	1			16	⊣ 8						Ш		
u_=-80					-2	2							2	-2					L_		-2	입			45	-38			-2	-2		
U _K =81					-2		2						2		-2						-2	ą	-2		-39	90	-39		-2	-3	-2	
U _L =96						-2	2				2	-2.		2		-2						-2	-2			-46	102	45		-2	-4	-2
U _M =-1,11					Ĺ						2	-2			2	-2											-52	56			-2	-2
U _N :24																													12	-11	Ш	
*U ₀ ==.13				L					<u> </u>	L		_			L						L_	<u> </u>				-1			-6	13		——
u _P 16																											l			7	16	7
u _o = .33											1	T			ı	-1								,			1	1			15	-17
RESIDUAL	0	ı	-3	-4	-3	2	١	0	2	0	3	-3	١	-1	-6	-1	ľ	3	0	2	-3	1	4	2	0	-1	-3	-3	-3	-4	-1	1
* V _D =-7.07			14	359			-14	-331											-14	-14	<u> </u>		14	14								
* Vp = 1.66										3	82	3		3	-95	3										3		-3		-3		3
*U _G = .09	T	Π																				4	-10	4			Ĺ					
* U _o =-,l35		Γ																								-1			6	14	-6	
FINAL RESIDUAL FORCES	0	I	-3	-2	-3	2	١	-2	2	0	-1	-3	ı	-1	-1	-1	1	3	0	2	-3	2	0	3	0	-l	-3	-3	-3	-ვ	4	1

TABLE 15. STRESS CALCULATIONS FOR MODEL WITH SINGLE CUTOUT.

CALCULATION OF STRESSES IN VERTICAL STRINGERS.

MEMBER Mn	V _{m TOT} X 10 ⁴	V _{η τοτ} × 10 ⁴	(\(\frac{1}{10}\) \(\frac{1}{10}\) \(\frac{1}{10}\) \(\frac{1}{10}\)	Kx10 ⁻⁴ LB./in.	STRESS PSI.
AE	-4.91	-2.75	2.16	375	810
DH	-7.07	-4.98	2.09	ч	785
EJ	-2.75	-1.06	1.69	11	634
нм	-4.98	-3.21	1.77	11	664
JN	- 1.06	.33	1.39	11	521
MQ	- 3.21	- 1.76	1.45	11	544
BF	27	0	.27	11	101
CG	27	.06	.33	. "	124
FK	0	.72	.72	11	270
GL	.06	.79	.73	11	274
ко	.72	1.74	1.02	Ш	382
LP	.79	1.66	.87	11	326

CALCULATION OF STRESSES IN HORIZONTAL STRIPS.

MEMBER MN	Ч _{П ТОТ} X Ю ⁴ .IN.	U _{N TOT} X 10 ⁴	(Un TOT - Um TOT)104	KxIO ⁻⁴ LB./IN. IN.2/IN.	STRESS PSI.
AB.	40	69	29	375	-109
ВС	69	-1.31	62	u	-232
CD	- 1.31	-1.67	36	н	-135
EF	47	35	.12	Ħ	45
FG	35	.09	.44	н	165
GH	.09	.35	.26	11	98
JK	ათ	81	- .01	u ·	-4
KL	81	96	15	18	-56
LM	96	~ 1.11	15	11	-56
NO	24	135	.105	11	39
OP	135	.16	.295	11	111
PQ	.16	.33	.17	И	64

TABLE 16. OPERATIONS TABLE FOR MODEL WITH DOUBLE CUTOUT. SHEET I.

DISP	L.	YA	YB	Yc	YD	YE	YF	የ ራ	YH	Y	Ϋ́ĸ	ኚ	YM	YN	Υ ₀	Ϋ́ρ	YQ	X	Хв	Χc	X_D	ΧĘ	Χ _F	Χ _G	Хн	ΧJ	X _K	X _L	Xμ	XΝ	X _o	ኢ թ	X_{Q}
V _A =	1	<u>50</u> 8	200		Г	468	200											욣	200			200	2.00									П	
V _E -	ı	46.8	260			016	400			3	2,00							231	200							2,00	200						
٧ _٧ -	ı					448	280			图	400			46,8	200							500	욃							200	2.00		
V _N =										48	200			508	200											<u> 2</u> 21	2 <u>60</u>			200	200		
VBLOCK	. 1	<u>\$</u>	480			<u>88</u> 0	800			휧	860			420	400			왕	욚			0	٥			0	0			400	400		
V _B -		28	57,2	2.00		Z.00	43 7	2.00										2,00		22		200		200									
V _F =	1	2.00	49.2	2,00		4.00	023	2.00		Z D O	48,1	0						200	0	28		0	200	200		<u> 200</u>	200	0					
V _K =	l .					200	48.1	0		400	023	200		2.00	49.2	200						200	200	$\lceil \rfloor$		0	200	<u>500</u>		200	0	200	
V ₀ =	1									200	49.2	200		200	<u>572</u>	200										200		200		<u>500</u>		200	
VBLOCK.	• I	400	t	L	<u>. </u>		-	400	<u> </u>		230	8		400	B <u>00</u>	400		480		옿		0	400	نــــا	L	0	400	4.00		400		4,00	
٧ _ç =	<u> </u>			<u>57.</u> 2					200					L					28		<u>500</u>		280		200		L						
V _G =	ł		280	49.2	200	L	200	<u>572</u>	200		Ŀ_			L		L			8	٥	200		욃	٥	200	_	L	L					
<u> </u>	1		L			Ĺ			L	L	200	ľ			<u> </u>		2.00					L		L_			200		230		500		2.00
V _P -			_				L		L		200						200			L				L_			200	┖	200		<u>200</u>		200
V _{BLOCK}		L		<u> </u>			4.00	_	4.00		4,00	82	400	L	400	<u></u>	400		8		100		<u>8</u>	<u> </u>	\$		4,00	L	3	<u> </u>	15		4.00
ν _D -				200	<u> </u>		L	<u>i</u>	46,8		L_		L	L	<u> </u>	L	<u>L</u>				2,00	_	_	_	2.00		<u> </u>	L	L_				
Ун -		<u> </u>		2.00	46.8	<u>_</u>	<u> </u>		229		L		471		_	L.				200	200		L	_	220		<u> </u>	0	0	_		\sqcup	
∀ _ =		<u> </u>	_		L	L		0	47,1			200				Ľ.	46.8							0	0	L		Ь	200				200
V _Q -	<u> </u>	L				L]_	200		L			5 <u>0.</u> 8							L				<u> </u>	2.00			200	
V _{BLOCK}	•			400	400			400	400			400	4.00			400	400			400	4.00			400	400			4.00	4,00			<u> 20</u>	400

UNDERLINED NUMBERS ARE NEGATIVE. FORCES IN LB., DISPLACEMENTS IN IN. X 10⁻⁴.

TABLE 16. OPERATIONS TABLE FOR MODEL WITH DOUBLE CUTOUT. SHEET 2.

DISPL.	Y _A	V	V	V	V	V	V	V	V	$\overline{\mathbf{v}}$	V	V	Y	Y	Y	Y	Υ.	Y.	Y	X.	X_	Y.	Y.	X.	X.	X	X.	x.	X	X.	x_	X _
DISFE.	'A	В	<u> 'C</u>	Q'	'E	"F	'G	'Η	٦,	'K	<u>'L</u>	M	Ż,	0'	P	_	_		_		_	-	_	H	Ĺ'n	' K	<u></u>	M	N	ď	4	°Q.
U _A = 1	2 <u>00</u>	2,00		L	200	200											500	448		L_	200	2.00										
U _B ≈ I	200		200		200		200										168	<u>01</u> 6	468		200	100	Z00				أحسا]			
U _C ₹ I		200		200		3		200										46.8	OL6	46.8		200	4 30	200								
U _D = I	T			200				2.00	-										46.0	50.8			260	200								
UBLOCK I	400			4.00													3	800	900	100	100	B,00	800	100								
U _E = I	200	200							200	200							200	200			558	478			200	200					∟_I	
U _F ~ I	200				0	200	200			8							200	4.00	200		47.8	1066	46B		Z00	2.00						
u _c - 1				200				200										200	400			168										
U _H = I				200				200			0	0							200	Z00			468	<u> 50,</u> 8			0	0				
UBLOCK = I	400	0				400	0	400	400	400							100	800	6.00	100	600	200	900	400	400	400						
U _J = 1	T	Γ	Γ	_	200		_						2	200			Г	Π		Γ	200	200		l	55.6	478			200	2,00		
U _K -I	T	T	†		200				0	200	200				200		Γ			T	200	200	0		478	1066	46.8		200	\$	Z 00	
U <u>.</u> = 1	1-	\vdash	✝	T	1	-	Г	T		200	_		_	_	-	2.00	Г	1	Π							46.8	101.6	468		200	400	200
U _M =1	╁	T	1	t		1	0	0		_		200		_	_	200		1	Γ	1			0	0	T		16.8	50.8			200	200
UBLOCK # 1	†	┢	\top	十	400	400	_	1	1	100						400		1	1	1	400	400		T	500	290	800	4.00	4.00	800	800	400
U _N = I	+-	┢	十	 	+	1	\vdash	╀	-	200	—~		200	┿~~	╁		t	†	┢	+-	十	 	1	1	+=	2.00		+=-	_	46.8	_	
U ₀ = 1	╁╴	╁~	╁	+	╁╴	╁┈	╁	╁	200		200	┢╌	200		200	 	1	十	\vdash	†	+	1-	1	T		400		—	_	101.6		
	╆╌	╁	+-	╁╌	╁─╴	┼-	╁╌	╁	F	200		200	_	200		200	\vdash	╂─	╁╌	╁╴	╁╌	╁╌	1	╁╌				200				46.8
u _р ~ 1	╀╌	╀	╂┈	╀	┼—	╀╌	╀	+-	╂			200		_		200		╂╌	╀	╂┈	╁	┢	╁	+	+		4	2.00	_		468	
u _o - 1	┼	╀-	╄-	╀	╄	↓_	╄	┡	-									╀	┈	╂	╀	┼	╀	╁	400		┺			_	_	_
UBLOCK I	<u>↓</u>	<u> </u>	1_	<u></u>		<u> </u>	<u>L</u>	<u></u>	100	0	10	400	1400	10	10	4.00		丄	<u> </u>	_		上			450	ĮΨV	auc	400		240	凹	떋

UNDERLINED NUMBERS ARE NEGATIVE. FORCES IN LB., DISPLACEMENTS IN IN. X 10-4.

TABLE 17. CHECK TABLE OF RELAXATIONS FOR MODEL WITH SINGLE CUTOUT WITH OPERATIONS PERTAINING TO MODEL WITH DOUBLE CUTOUT. SHEET I.

DISPL.	Y _A	Ϋ́Β	24	YD	ΥE	¥	YG	Y _H	Y	YK	YL	¥	×	ሃ	Ϋ́P	24	X	ΧB	Xc	X _D	Χ _E	Χ÷	X_{G}	ΧH	ΧJ	Xĸ	X _L	X _M	׎	Χo	ኢ _ዮ	X_Q
EXTERNAL LOADS	124			124									62	62	82	62																
V _A =-4.9l	Z50	-10			730	-9											10	10			-10	40										
V _E -2.75	129	-6			279	-31			-129	-6							6	6							-6	-6	Γ					
V _J ≠−l.06					-50	-2			100	-4			-50	-2							2	2							-2	-2		
V _N = .33									15	1			-17	1											-1	-1	Γ			1		
V _B =27	- I	15	-1		- 1	-13	-1										-1		١		١		-1									
V _F = 0	Г																										Г					
V _K 72					1	35			3	-79	-		ī	35	-						1	١				-1	-1		-1		T	
V ₀ = 1.74									3	86	3		3	100	3										3		-3		-3		3	
Vc=-27		-1	15	-1		-1	-13	- I										-1		1		1		-1								
V _G 06		`	3				-3																				Γ					
V _L 79						-				2	-45	2		2	39	2										2		- 2		-2		2
V _P = 1,66										3	82	3		3	95	3										3		-3		-3	П	3
V _D =-7.07			-14	359			14	-331											-14	-14			14	14			Γ				\Box	
V _H =-4,98			-10	Z 33			-10	488				135							10	10			10	10								
V _M =~3.21								151			-6	314			-6	150											-6	-6			6	6
Vo=-1.76											-4	-82			-4	89											-4	-4			4	4

TABLE 17. CHECK TABLE OF RELAXATIONS FOR MODEL WITH SINGLE CUTOUT WITH OPERATIONS PERTAINING TO MODEL WITH DOUBLE CUTOUT. SHEET 2.

DISPL.	Y	YB	Yc	YD	YE	Y _F	YG	Y,	Υ _J	Yĸ	Ϋ́	Y _M	Y	γo	Yp	S.	X,	XΒ	Χ _C	X_D	Χ _E	X _F	Χ _G	X _H	ΧJ	Xĸ	X _L	X,	X	Χo	ኢ	XQ
U _A =40	ī	-1			ı	-1											20	-19			-1	-1										
U _B =69	1		-1		ı		-1										-32	70	-32		1	-3	-1									
U _c =-1.31		3		-3		3	Γ	-3										61	133	-61		-3	-5	-3								
u _p 1.67			3	-3			3	-3											-78	85			-3	-3								
U _E 47	-1	-				Γ			1	-+							-1	-1			26	-22			-1	- 1						
U _F =-;35	-1		ī			-1	T			-1							-1	-1	-1		-17	37	46		-1	-1						
u _G 09						Γ																4	-9	4								
U _H 35			٦	-1		Г	П	-1											ı	ī			16	-18								
u,=80					-2	2							2	-2		-					- 2	-2			45	-38			-2	-2		
18,,u					-2	2				2	-2		2		-2						-2	-2			-39	86	-38		- 2	-3	-2	
u _L =96										2		-2		2		-2				Ι						-45	98	45	•	-2	-4	- 2
u _M =−I.II							П				2	-2			2	-2											-52	56			-2	-2
U _N =24							Г						Г																12.	-11		
u _o =-135							Г																			-1			-6	14	-6	
u _p - J6			Г				Π														Γ						Ī			7	-16	7
U _Q = .33			Г		Γ				一		-	-1			1	-1											ī	1			15	-17
RESIDUAL	-4	1	-3	-6	-3	3	-37	-2	2	5	32	-3	3	1	١	1	Ī	3	0	2	-3	2,	5	3	0	-3	-4	-3	-3	-3	-1	١

TABLE 18. RELAXATION OF RESIDUAL FORCES FOR MODEL WITH DOUBLE CUTOUT. SHEET 1.

DISPL.	YA	YΒ	Yc	Ϋ́D	YΕ	YF	YG	式	۲Y	Υĸ	ΥL	Ϋ́м	Y	οĄ	완	ōΚ	X	Хв	Xc	X_D	Χ _E	X_{F}	X_G	XΗ	ΧJ	Xĸ	X_{L}	Xμ	X	X_{O}	Χ _P	X
RESIDUAL FORCES	-4			-6	-3	3	-37	-2	2	5	32	- 3	3	1	I,	1	ı	3	0	2	-3	2	5	3	0	-3	-4	-3	-3	-3	-1	-
Vc=-31	1	-1	-15	-1			18											-1		1												
Vc-Vg=-2.25		0 -9	-18 18	-7 -9		2 -9		_ე -ე										·2 -9		13 9		3		2 -9								
V∟ = .30		-9	0	-16		-7	-1	-12		_	-17	١		١				-7		12		12		-7				-1		-1		
V <u>L</u> *Vp * I.88							_				-15	-2 8			-15	Ø										-2 8	Ĺ	-4 -8		-4 -8		2 8
VB=17		10				-8				14	0	6		10	1	10										6		-12		-12		10
V _K = .33		-			_	15 16			1	-36	ı		ı	16							-	-				-1	~1	ł .	-1		ı	
Vo = 45					-2	•			3	22				-26	_t						-2	13			1	5	-5 -1		-4 -1		0-	
V _A ~08	4				-4		Γ		4	0	2		5	0	3												-6		-5		-	
8l. – LV	0				-6				-13				6																			
V _N = .22					0				- 9 10				77																			
Vp==.28			-1	14				-13					O						-1	-1			١									
Vq - .20			-1	-2			-2	-25				•				-10			-1	11			6	-6			,	,			-1	
V _D V _H - 49			-2	2			-2					15 -23				0			- 2	-2			2	2		Γ	-5	-11			٥	9
VM=-06			-3	o			-4	0 -3				-8 6				-3			-3	9		-	8	-4			-5	-11			0	9
V <u>1</u> -V _P + .25								-3		1	-2	- N -		1	-2		L									[i		-1		- 1		1
v _D = .02				-1				ı		1	0	-		١	'	-Z																
VcVc~~25		-1	2	I I		-1	2	-2 -1										-1		[i		ī		-1								
RESIDUAL	0	0	<u>-ī</u>	-2	0	0	-2	-3	1	1	0	-1			1	-2		-8 S #		10	-5		В	-5	Ī	6	-5	-12	-5	-13	0	10

TABLE 18. RELAXATION OF RESIDUAL FORCES FOR MODEL WITH DOUBLE CUTOUT. SHEET 2.

DISPL.	Y _A	Ϋ́В	Yc	Ϋ́D	YE	YF	YG	Ϋ́́́	Υ _J	Ϋ́κ	YL	YM	ΣŽ	٧	Ϋ́Р	δ<	Χ _A	Хв	X_{C}	ΧĐ	ųΨ	X _F	Χ _G	춋	ΧJ	Xĸ	X_{L}	×	Ž	Χo	Xφ	Χo
RESIDUAL FORCES	٥	0	-1	-2	0	0	-2	- 3	1	_	٥	-1	0	_	_	- 2.	1	-8	-3	10	-2	14	8		1	6	-5	-12	-5	-13	0	10
U _H =10																		L_					-5	5								
u _F =06							<u> </u>											L			-3			٥								
u _E =21																					-5 12	20 -11										
U _M =24																					7	9					-11	12.				
u _K = .34			-,		1	-1				-1	ı		-1		1						1	ī			16	36	-16 16	0	1	١	١	
u ₁ 44					1	- <u>1</u>				0	ī		=1	1	2						8	10			17 -25	-30 21	0		-4 1	-12 1	١	
U _{ABCD} = U _{EFCH} 2.00					2 -8	-2 8			-8	8			-2	2							-8	-8			-8 8	9 8			-3	-11		
u _c = .17					-6	6		T	-7	8								8	-17	8	1	3	1		0	-1						
U _D = .38	┢			<u> </u>	 				-							一		O	-20 18	18 -19			 	<u> </u>								
U _N =04		T		┞	 			<u> </u>								T			-2	-1			ļ				Γ		2	-2		
U _p = .24		T			_		\vdash			Г	-	-	T		Г						ļ.—.						1		-1	-13 11	-24	
U _Q = .4,4	T	T								_			T					厂	T			\vdash	T				T			-2		21 -22
V _{AEJN} =50	0 2	0 -2		-2	-6 4			-3	-7 4			-1	-2 2			-2	1 2		-2	-1	<u> </u>	3	1	0	0	1	1	0	-1 -2		-2	-1
VAEJN .50 VAE-VB- VNVO-04	2	-2 2		 	-2 2	2			-3 2	4	1		0	0			3	_1				 	T				<u> </u>			-4		
RESIDUAL.		0		-2		1.		-3	1		J	-1	-2			-2	3	2	-2	-1	1	3	1	0	0	-1	1	0	-3	-4	-2	-1

TABLE 19. COMPLETE CHECK TABLE FOR MODEL WITH DOUBLE CUTOUT.

* ADJUSTED VALUES APPEAR AT END OF TABLE. SHEET I.

DISPL.	YA	Ϋ́в	Ϋ́c	Ϋ́D	Ϋ́E	Y _F	Ϋ́G	Υ _H	۲ _ر	Yĸ	Ϋ́	Y _M	Ϋ́Z	Yo	Ϋ́P	YQ	X _A	Хв	Χ _C	X_D	Χ _E	X _F	X _G	Хн	ΧJ	Xĸ	X _L	XΜ	XN	Χo	Χ _P	XQ
EXTERNAL LOADS	124			H2A									62	62	62	62															-	
V _A =~5.45	277	-11			-255	Ξ			. _								11	Ξ			-11	1										
V _E =-3.25	152	-7			330	-13			-152	-7							7	7							-7	-7						
V _J =-143	Π				-67	- 3			145	-6			-67	-3			•				3	3							-3	-3		
V _N = .09	Π								4				-5																			
V _B =48	-1	27	-1		-1	-24	-1										-1		1		1		-1								_	
*V _F - 0																												·				
VK - 1.05					2	51			4	-115	2		2	52	2						2	2				-2	-2		-2		2	
*V ₀ = 2.15									4	106	4		4	123	4										4		-4		-4		4	\Box
V _C =-2.77		-6	158	-6		-6	136	-6			_							-6		6		6		-6								
V _G =-2.75		-6	-135	-6		-6	157	-6										-6		6		6		-6								
V _L = 3.22										6	184	6		6	158	6										. 6		-6		-6		6
V _P = 3.79			<u> </u>							8	186	8		8	-217	8										8		-8		-8	-	8
×V _D = -7.82		i.	-16	397			16	366											-16	-16			16	16								
*V _H =-5.47			-11	-256			-11	536				-258							-11	-11			11	11							\neg	П
V _M ~~3.27								154			-7	320			-7	1 53											-7	-7			7	.7
*Vq=-1.56	T		Г						Г		~3	-73			-3	79											-3	-3			3	3
UA = 1.60	-3	3	<u> </u>		-3	3											81	75		<u> </u>	3	3				-					\neg	
U _B = 1.31	-3		3		-3	Γ	3		Γ								61	133	61		3	5	3			_			<u> </u>		\neg	\Box
U _C = .86		- 2		2		-2		2	Г									40	-87	40		2	3	2			Г				\neg	
U _D 71			-1	I			-1	T											33	-36			1	Ī							7	\square

TABLE 19. COMPLETE CHECK TABLE FOR MODEL WITH DOUBLE CUTOUT.

* ADJUSTED VALUES APPEAR AT END OF TABLE. SHEET 2.

			·		_	-												_	_	_	_								-			
DISPL.	YA	YΒ	Yc	Y_{D}	YE	YF	Ϋ́	Y_H	Υ _J	Yĸ	YL	YΜ	Y 2	Yo	Y_P	YQ	ΧĄ	Хв	x_c	χĐ	Χ _E	X_F	X_G	XH	X_J	Xĸ	X_L	Xμ	X_N	X_{O}	X_P	X_{Q}
U _E = 1.32	3	-3							-3	3							3	3			-74	63			3	ფ						
*U _F = 1.59	3		-3			3	-3		-3	3							3	6	3		76	169	74		3	ფ						
U _G - 2.09		4		-4		4		-4										4	8	4		98	-212	98								
U _H -2.25			5	-5			5	-5											5	5			105	114								\Box
U _J =−.36					-1	_							i	-1							-1	-1			20	-17			-1	-1		
U _K =47					-1	1				-	-1		1		-1						-1	-1			-22	50	-22		-1	-2	-1	
u96										2		-2		2		-2										45	98	-45		-2	-4	-2
U _M =-1.35											3	-3			3	-3											-63	69			-3	-3
U _N =+.28									-	1			-1	1											-	- 1			14	-13		
υ _ο =ι3																										-1			-6	13	-6	
U _P = .40										-		-1		1		1				Γ						1	2	_ I		19	41	19
$U_{Q} = .77$									_		2	-2			2	-2.											2	2			36	-39
RESIDUAL	0	- 1	-1	-1	1	-2	-3	-2	-2	3	2.	-5	-3	5	3	-6	3	_	-3	-2	1	6	0	2	0	-2	1	3	-3	-3	-3	-1
*U _F = 1.61	3		-3			3	-3		-3	3							3	6	3.		77	H72	75		3	3						\Box
*V _F =04			-2			4			_	-2																						
* V ₀ = 2.18									4	107	4		4	-125	4										4		-4		-4		4	
× √ _D =-7.78			⊣6	395			-16	-364											∓6	-16			16	16								
*V _H -5.44			-11	-255			-11	533				-256							-11	-11			11	П								
* VQ=-1.59											-3	-74			-3	81											-3	3			3	3
FINAL RESIDUAL FORCES	0	-1	-3	-2	١	2	-3	-3	-2	2	2	-4	-3	3	3	-4	3	l	-3	-2	2	3		2	0	-2	١	3	-3	-3	-3	-1

TABLE 20. STRESS CALCULATIONS FOR MODEL WITH DOUBLE CUTOUT.

CALCULATION OF STRESSES IN VERTICAL STRINGERS.

MEMBER MN	V _{m TOT} X 10 ⁴	V _{n тот} хю ⁴	(√ _{n тот} – √ _{m тот}) 0⁴	KXIO-4 LB. IN.2/IN.	STRESS PSI.
AE	- 5.45	- 3.25	2.20	375	825
DH	-7.78	- 5.44	2.34		878
EJ	- 3.25	- 1.43	1.82	11 .	683
НМ	- 5.44	- 3.27	2.17	ц	814
JN .	- 1.43	.09	1.52	ı.	570
MQ	- 3.27	- 1.59	1.68	*	630
BF	48	04	.44	×	165
CG	- 2.77	- 2.75	.02	•	8
FK	04	1.05	1.09		409
KO	1.05	2.18	1.13	×	424
LP	3.22	3.79	.57	l1	214

CALCULATION OF STRESSES IN HORIZONTAL STRIPS

MEMBER M N	U _{m TOT} X 10 ⁴	U _{n TOT} X 10 ⁴	(U _{n TOT} - U _{mTOT})10 ⁴	Kx10 ⁻⁴ LB. IN. ² /IN.	STRESS PSI.
AB	1.60	1.31	29	375	-109
ВС	1.31	.86	45	11	-169
CD	.86	.71	15	11	- 56
EF	1.32	1.61	.29	n	109
FG	1.61	2.09	.48	N	180
GH	2.09	2.25	.16	ĸ	60
JK	36	47	11		- 41
KL	·47	96	49	Iŧ	-184
LM	96	1.35	39	u	-146
NO	28	13	.15	11	56
OP	13	.40	.53	w	199
PQ	.40	.77	.37	1	139

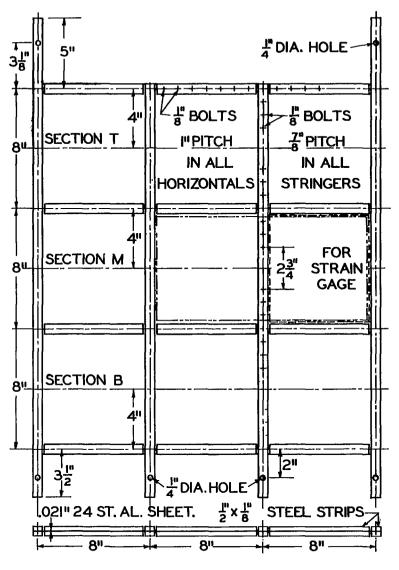
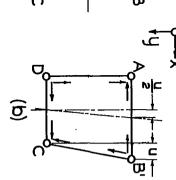
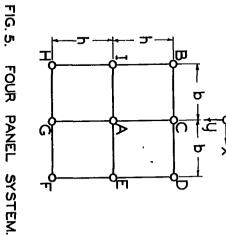


FIG. I. MODEL TESTED. LOCATION OF SINGLE CUTOUT. LOCATION OF DOUBLE CUTOUT.

ARROWS INDICATE DIRECTION OF SHEARING FORCES TRANSMITTED FROM SHEET TO CONSTRAINTS. UNIT OF <u>0</u> REINFORCED SHEET





FOUR PANEL

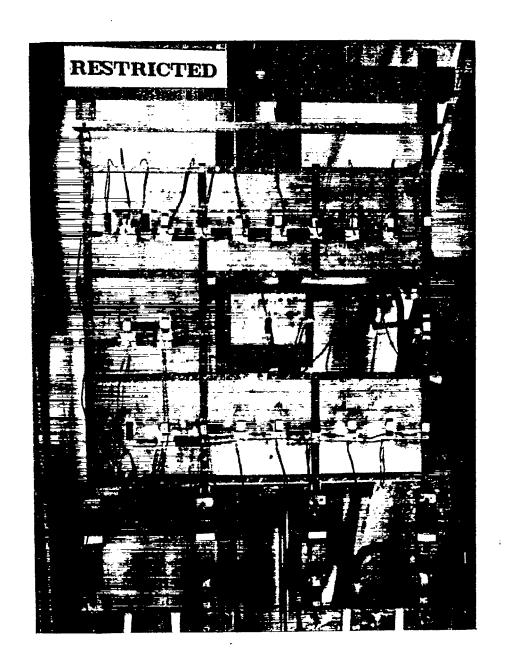


Figure 2.- Front view of test setup.



Figure 3.- Three-quarter view of test setup.

FIG. 6. SCHEMATIC DRAWING OF MODEL WITHOUT CUTOUT.

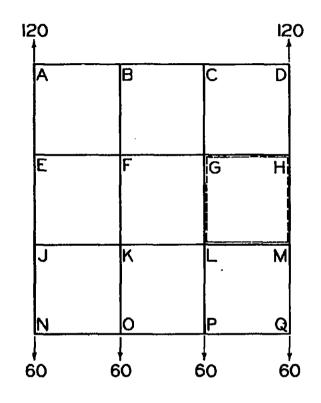


FIG. 7. SCHEMATIC DRAWING OF MODEL
WITH SINGLE CUTOUT.
------ LOCATION OF CUTOUT.

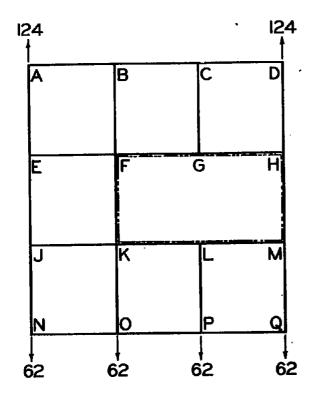


FIG. 8. SCHEMATIC DRAWING OF MODEL
WITH DOUBLE CUTOUT.
LOCATION OF CUTOUT.

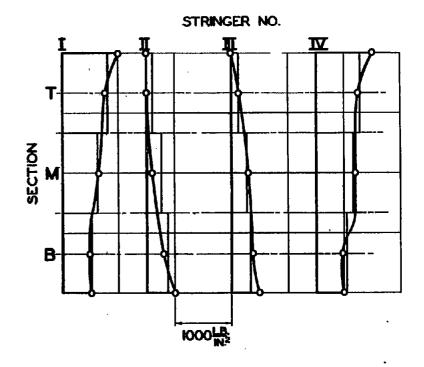


FIG. 9. CALCULATED AND MEASURED DIRECT STRESS IN STRINGERS FOR MODEL WITH SINGLE CUTOUT.

O MEASURED VALUES
------- CALCULATED VALUES.

Figs. 8.

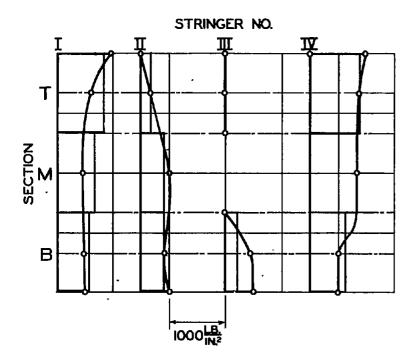


FIG. 10. CALCULATED AND MEASURED DIRECT STRESS IN STRINGERS FOR MODEL WITH DOUBLE CUTOUT.

MEASURED VALUES.
 CALCULATED VALUES.

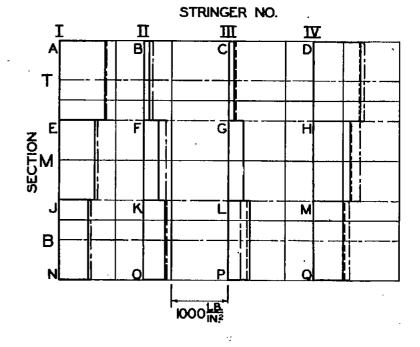


FIG.11. COMPARISON OF CALCULATED DIRECT STRESS
IN STRINGERS FOR THE THREE
MODEL CONDITIONS,

FOR MODEL WITH NO CUTOUT.

FOR MODEL WITH SINGLE CUTOUT.

FOR MODEL WITH DOUBLE CUTOUT.

Figs. 10, 11

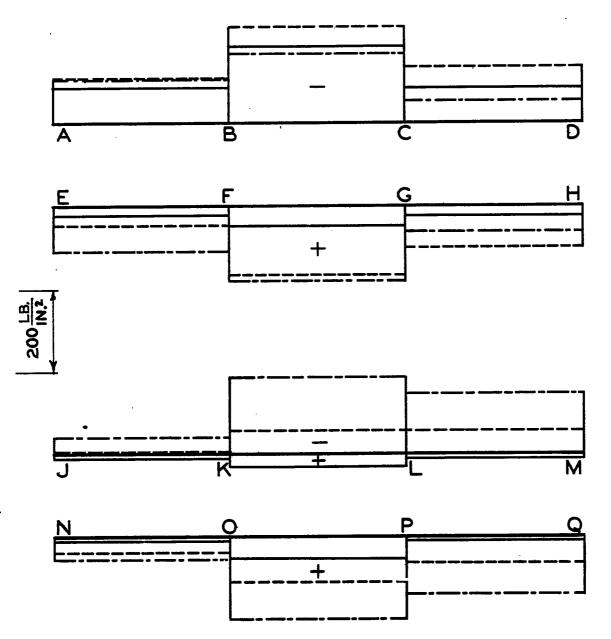


FIG. 12. COMPARISON OF CALCULATED DIRECT STRESS IN HORIZONTAL STRIPS FOR THE THREE MODEL CONDITIONS.

FOR MODEL WITH NO CUTOUT.

FOR MODEL WITH SINGLE CUTOUT.

FOR MODEL WITH DOUBLE CUTOUT.

.3